

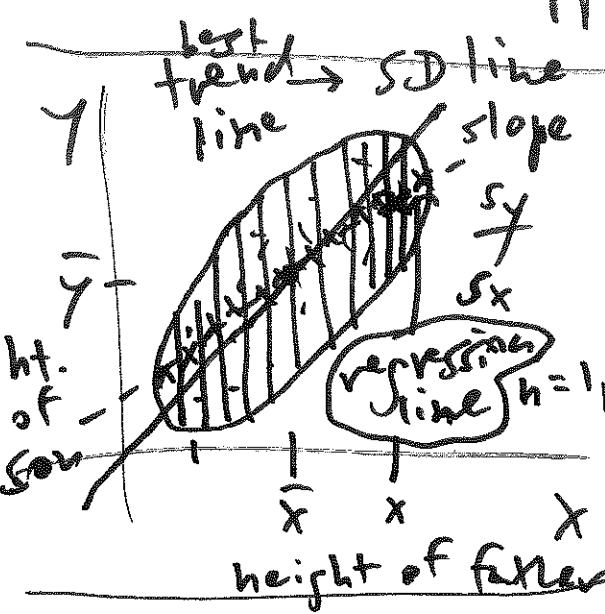
this regression  
 time:  $\downarrow$   
 next  
 time: ANOVA

read: LN pp. L-245  
 L-274  
 AMS7  
 31 May  
 I am cancelling homework ①  
 homework 4 due 11.59pm Fri

there will be either 1 or 2 make up  
 lectures in finals week, on Mon (& Tues).  
 more details soon

take home final handed out  
 in class Fri 9 Jun, due  
 1 week later

exact 95% CI  
 method: LN pp. L-231 + L-244



simple linear regression

Q: slope, intercept  
 of best line?

A: Q: best in what  
 sense?

Gauss (1800)  
 Galton (1890)

A: best line for  
 predicting y from x

(best line  
 for pred. x from y)

(best  
 trend line)

slope of regression line

$$\hat{\beta}_1 = r \cdot \frac{s_y}{s_x}$$

equation (17)

p. R-25

equation of regression line

$$\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x$$

↑  
predicted y value

↑  
y-intercept

reg. line goes through  $(\bar{x}, \bar{y})$

$$\bar{y} = \hat{\beta}_0 + \hat{\beta}_1 \bar{x}$$

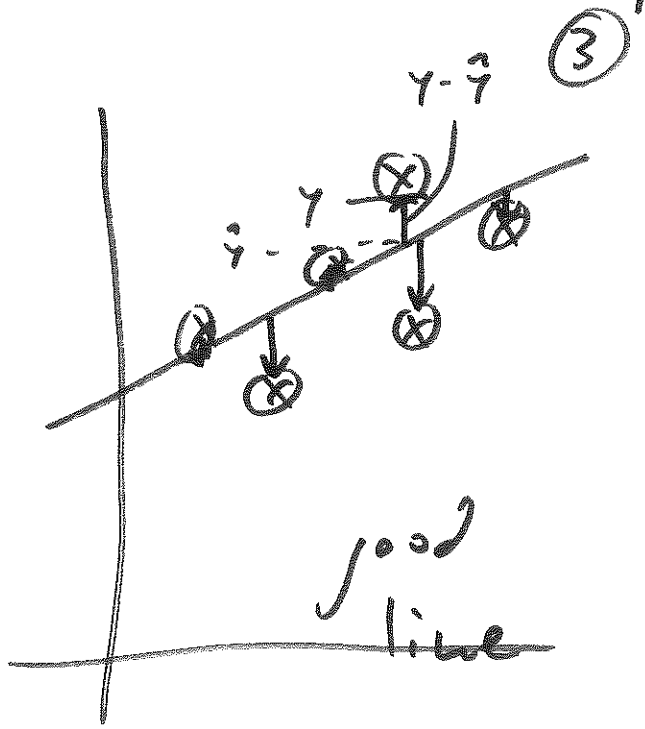
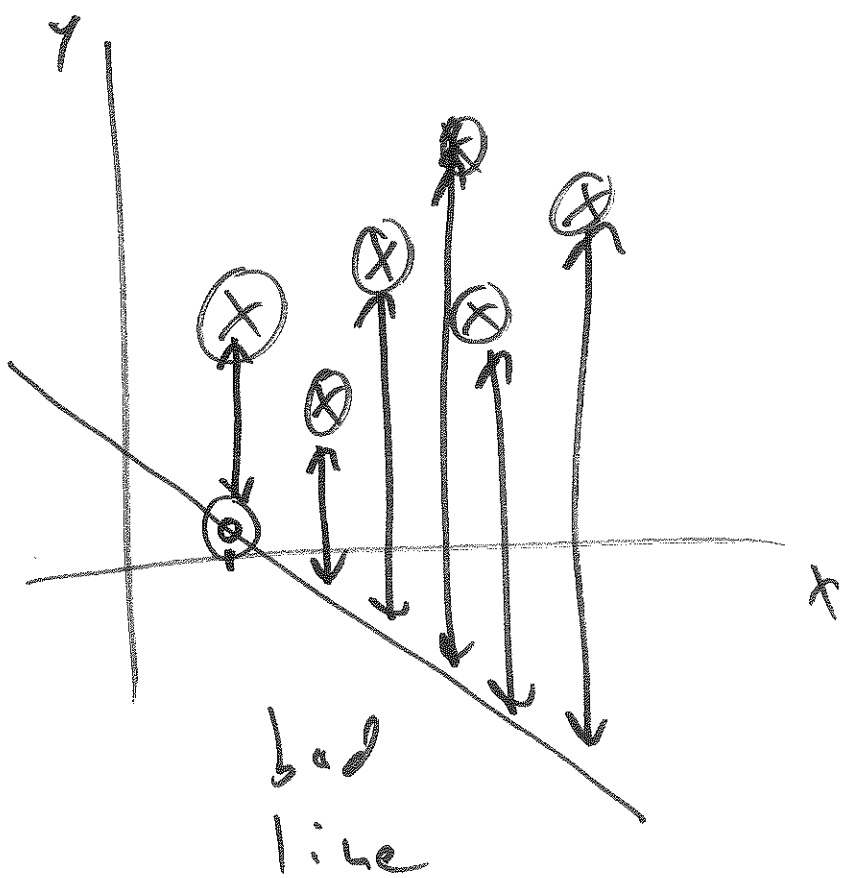
so

$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$$

eqn. (21)

p. R-25

regression to the mean



best line solver  
 2D problem:

find  $(\hat{\beta}_0, \hat{\beta}_1)$   
 to minimize

$$\frac{1}{n} \sum_{i=1}^n \left[ y_i - (\hat{\beta}_0 + \hat{\beta}_1 x_i) \right]^2$$

Gauss  
 Laplace

$y_1$	$x_1$
$\vdots$	$\vdots$
$y_i$	$x_i$
$\vdots$	$\vdots$
$y_n$	$x_n$

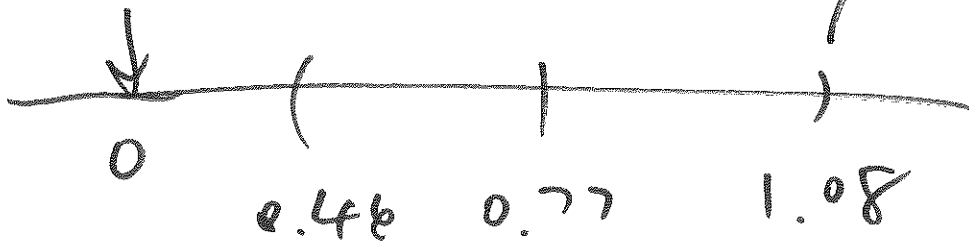
$$\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x$$

math fact

regression line =

least squares lines

95% CI for  $\beta_1$



the diff <sup>(4)</sup>  
between  
0.77 & 0

(15) statistic