

Disc. Sec. week of 5-9 Jun 2017

DS 9 #1 p. R-74

Ans 7
5 Jun 17
①

just like wing length / tail length from class. correlation & regression

$$r = -0.9904$$

$$^{\circ}F = \frac{9}{5}(^{\circ}C) + 32^{\circ}$$

$$r = \frac{1}{n} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x^*} \right) \cdot \left(\frac{y_i - \bar{y}}{s_y^*} \right)$$

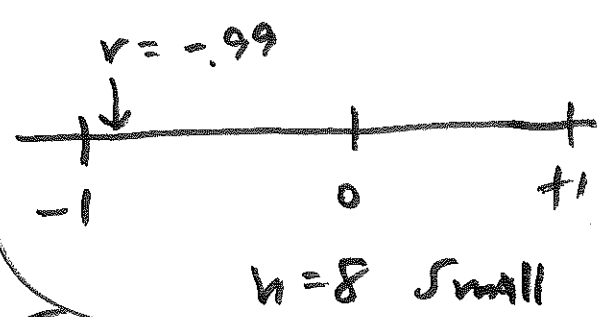
(b) $r =$ same for temp. in $^{\circ}F$ as in $^{\circ}C$

$$SE(r) = \sqrt{\frac{1-r^2}{n-2}}$$

formula (16), p. R-25

$$= \sqrt{\frac{1 - (-.9904)^2}{8-2}}$$

$$= 0.056$$



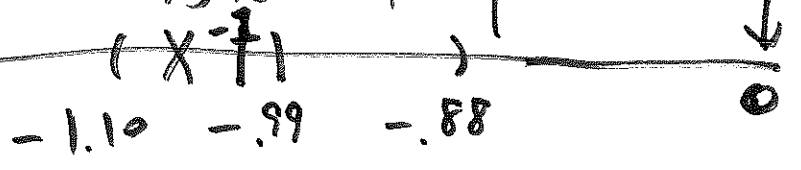
approx. 95% CI:

$$r \pm 2 SE(r)$$

$$-.9904 \pm 2(.056)$$

95% CI for ρ

(-1, -.88) is approx. 95% CI



since 0 not in 95% CI, diff. $\hat{\rho}$ \neq 0
 between $r = -.99$ & $\rho_0 = 0$ (is) (highly)
 stat sig. \hat{r} is (highly) \neq 0
 & r is \neq 0

regression line
 for predicting
 $y = \text{oxygen}$
 from $x = \text{temperature}$

$$\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 \cdot x$$

$$\hat{\beta}_1 = r \frac{s_y}{s_x}$$

formula (17), p. R-25

$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$$

(formula (21), p. R-25)

$$= (-.9904) \frac{1.1285 \text{ w/g/hr}}{12.74 \text{ }^\circ\text{C}}$$

$$= 3.625 \text{ w/g/hr}$$

$$= \text{~~0.09904~~ } = -.0877 \text{ w/g/hr}$$

$$= 3.47 \text{ w/g/hr}$$

$$- (-.0877) \cdot (-1.75) \text{ }^\circ\text{C}$$

(w/g/hr) \cdot (°C)

reg. line for pred
 ox. from temp:

$$\hat{y} = 3.47 - .0877x$$

(c) (iii) predict y when $x = \underline{-15^\circ\text{C}}$ ③
& attach a $\hat{\sigma}_E$ to the prediction

$$\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x = 3.47 - .0877(-15) \\ = 4.79 \text{ mg/l/h}$$

$$\hat{\sigma}_E(\hat{y}) = s_y \sqrt{1-r^2} \sqrt{\frac{n-1}{n-2}}$$

formula (24),
p. R-26

$$= 1.1285 \sqrt{1-(.9904)^2}$$

$$\cdot \sqrt{\frac{2}{26}}$$

$$= 0.17 \text{ mg/l/h}$$

$$= \text{RMSE}$$